

Comparison of Five Numerical Methods for Computing Quality Factors and Resonance Wavelengths in Photonic Crystal Membrane Cavities

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The photonic crystal (PhC) membrane represents a platform for planar integration of components, where cavities and waveguides may play a key role in realizing compact optical components with classical functionality such as switches, lasers, and amplifiers or quantum optical functionality such as integrated sources of quantum light. By leaving out a row of holes in an otherwise perfect PhC membrane lattice, a line defect is created in which light may be guided. If the waveguide is terminated at both ends, the finite-length waveguide forms an L_n cavity, where n denotes the length of the cavity. Such L_n cavities support spectrally discrete optical modes, and the fundamental cavity mode profile of an L_9 cavity is shown in Fig. 1. Light may be confined to such an L_n cavity for extended periods, as quantified by the quality (Q) factor. For laser applications, the Q factor governs the onset of lasing, and for cavity quantum electrodynamics applications, it governs the onset of strong coupling. The Q factor thus represents a key parameter in the design of a PhC membrane cavity.

The combination of the large size of the PhC L_n cavity and the full 3D nature of the geometry makes the calculation of the cavity Q factor an extremely demanding numerical challenge. No matter which numerical method is used, careful convergence checks with respect to the degrees of freedom must be made. Additionally, most numerical simulations methods rely on a closed simulation domain, and here the influence of the boundary conditions requires carefully study. A study of PhC nanobeam cavities using four numerical techniques has previously been reported [1], where cavity frequencies and Q factors were investigated as function of structural parameters. While qualitative agreement between the methods was found, quantitative discrepancies were in some cases as large as an order of magnitude, and estimates for the computational error and the influence of the size of the computational domain were not given.

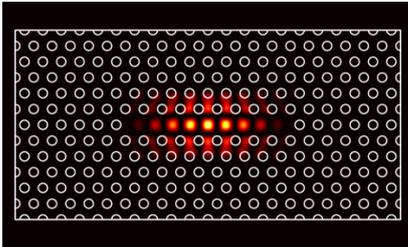


Fig. 1: Optical field $|E_y|^2$ profile for the L_9 cavity mode.

Table 1: Calculated Q factors and resonance wavelengths λ .

	FDTD	FDFD	FEM	SIE	FMM
λ^{L5} (nm)	1568	1572	1571	1572	1567
λ^{L9} (nm)	1574	1580	1578	1579	1570
Q^{L5}	1670	1725	1705	1707	1700
Q^{L9}	104,000	108,000	105,000	104,000	60,000

In this work, we focus on two structures, a low-Q L_5 cavity and a high-Q L_9 cavity. We employ five different computational methods [2], the finite-difference time-domain (FDTD) technique, the finite-difference frequency-domain (FDFD) technique, the finite-element method (FEM), the surface integral equation (SIE) approach and the Fourier modal method (FMM), to compute the cavity Q factor and the resonance wavelength for both structures. For each method, the relevant computational parameters are systematically varied to quantify the computational errors. In particular, we investigate the influence of the size of the computational domain. The final results summarized in Table 1 show that the resonance wavelengths agree fairly well for the two geometries among the five methods. On the other hand, significant deviations are observed for the Q factor. Our study highlights the importance of careful convergence checks and systematic estimation of the computational error, both of which are generally missing in the literature.

References

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